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generating proposals by utilizing the input data, each said proposal comprising a collection of bids that can be awarded to a player participating in the auction, said bids being actual bids made and being considered simultaneously;

selecting a set of proposals such that each item is included in at most one selected proposal; and

informing the players bidding on the items of the result of said selecting a set of proposals.



- 4. (Twice Amended) A method according to claim 1, wherein said selecting a set of proposals is enabled by using an integer programming technique.
- 6. (Twice Amended) A method for selecting a set of bids in a combinatorial auction for at least two items involving at least one player and at least one type of bid for each player such that:
 - (a) each item is contained in at most one (or exactly one) selected bid;
- (b) for each player, the selected bids all belong to the same type; and among all collections of bids satisfying (a) and (b) the selected bids maximizing total revenue, said method comprising:

generating all valid proposals, said proposals comprising a collection of bids that can be awarded to a player participating in the auction, said bids being actual bids made and being considered simultaneously;

formulating an integer program that includes a column for each proposal, a constraint for each item and a constraint for each player, said constraints representing conditions (a) and (b)

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respectively, and an objective function which represents revenue;

solving the integer program for selecting the set of proposals that maximizes revenue;

and

constructing a set of winning bids from the set of winning proposals.

- 8. (Twice Amended) A method for selecting a set of bids in a combinational auction for at least two items involving at least one player and at least one type of bid for each player such that
 - (a) each item is contained in at most one (or exactly one) selected bid;
- (b) for each player, the selected bids all belong to the same type;
 and among all collection of bids satisfying (a) and (b) the selected bids maximized total revenue,
 said method comprising:

generating a set of valid proposals, each said proposal comprising a collection of bids that can be awarded to a player participating in the auction, said bids being actual bids made and being considered simultaneously;

formulating an integer program that includes a column for each proposal, a constraint for each item and a constraint for each player, said constraint representing conditions (a) and (b) respectively, and an objective function which represents revenue;

solving a linear programming relaxation of the integer program in said formulating an integer program for obtaining dual variables associated with each of the constrains;

using dual variables obtained in said solving a linear programming relaxation for determining the excess value associated with each bid, and a threshold for each player;



4

using a proposal generation method for selecting each player and type, a proposal for which the excess value exceeds the threshold, or determining that no such proposal exists;

adding the proposal generated in said using a proposal generation method and repeating said solving a linear programming relaxation, said using dual variables, and said using a proposal generation method until no new proposals are identified;

solving the integer program that includes all identified proposals; and constructing a set of winning bids from the set of winning proposals.

9. (Twice Amended) A program storage device readable by a machine, tangibly embodying a program of instructions executable by the machine to perform method steps for executing a combinatorial auction, said method steps comprising:

reading input data comprising:

- a plurality of items;
- a player bidding on the items; and
- a plurality of bids, where each bid specifies the player bidding, the amount bid, and the list of items included in the bid;

generating proposals by utilizing the input data, each said proposal comprising a collection of bids that can be awarded to a player participating in the auction, said bids being actual bids made and being considered simultaneously;

selecting a set of proposals such that each item is included in at most one selected proposal; and

informing the players bidding on the items of the result of said selecting a set of proposals.

- 10. (Twice Amended) A computer comprising:
 - (1) means for reading input data comprising:
 - a plurality of items;
 - a player bidding on the items; and
- a plurality of bids, where each bid specifies the player bidding, the amount bid, and the list of items included in the bid;
- (2) means for generating proposals by utilizing the input data, each said proposal comprising a collection of bids that can be awarded to a player participating in the auction, said bids being actual bids made and being considered simultaneously;
- (3) means for selecting a set of proposals such that each item is included in at most one selected proposal;
- (4) means for informing the players bidding on the items of the results in said means for selecting.



VERSION WITH MARKINGS TO SHOW CHANGES MADE

IN THE CLAIMS:

- 1. (Twice Amended) A method for executing a combinatorial auction, the method comprising:
 - [(1)] reading input data comprising:
 - [(i)] a plurality of items;
 - [(ii)] a player bidding on the items, and
- [(iii)] a plurality of bids, where each bid specifies the player bidding, the amount bid, and the list of items included in the bid;
- [(2)] generating proposals by utilizing the input data, each said proposal comprising a collection of bids that can be awarded to a player participating in the auction, said bids being actual bids made and being considered simultaneously;
- [(3)] selecting a set of proposals such that each item[s] is included in at most one selected proposal; and
- [(4)] informing the players bidding on the items of the result of said selecting a set of proposals.
- 4. (Twice Amended) A method according to claim 1, wherein [step (3)] said selecting a set of proposals is enabled by using an integer programming technique.

- 6. (Twice Amended) A method for selecting a set of bids in a combinatorial auction for at least two items involving at least one player and at least one type of bid for each player such that:
 - (a) each item[s] is contained in at most one (or exactly one) selected bid;
- (b) for each player, the selected bids all belong to the same type;
 and among all collections of bids satisfying (a) and (b) the selected bids maximizing total revenue,
 said method comprising:
- [(1)] generating all valid proposals, said proposals comprising a collection of bids that can be awarded to a player participating in the auction, said bids being actual bids made and being considered simultaneously;
- [(2)] formulating an integer program that includes a column for each proposal, a constraint for each item and a constraint for each player, said constraints representing conditions (a) and (b) respectively, and an objective function which represents revenue;
- [(3)] solving the integer program for selecting the set of proposals that maximizes revenue;

and

- [(4)] constructing a set of winning bids from the set of winning proposals.
- 8. (Twice Amended) A method for selecting a set of bids in a combinational auction for at least two items involving at least one player and at least one type of bid for each player such that

 (a) each item[s] is contained in at most one (or exactly one) selected bid;

(b) for each player, the selected bids all belong to the same type;

and among all collection of bids satisfying (a) and (b) the selected bids maximized total revenue, said method comprising:

- [(1)] generating a set of valid [porposals] proposals, each said proposal comprising a collection of bids that can be awarded to a player participating in the auction, said bids being actual bids made and being considered simultaneously;
- [(2)] formulating an integer program that includes a column for each proposal, a constraint for each item and a constraint for each player, said constraint representing conditions (a) and (b) respectively, and an objective function which represents revenue;
- [(3)] solving a linear programming relaxation of the integer program in said formulating an integer program for obtaining dual variables associated with each of the constrains,
- [(4)]using dual variables obtained in said solving a linear programming relaxation for determining the excess value associated with each bid, and a threshold for each player;
- [(5)] using a proposal generation method for selecting each player and type, a proposal for which the excess value exceeds the threshold, or determining that no such proposal exists;
- [(6] adding the proposal generated in said using a proposal generation method and repeating said solving a linear programming relaxation, said using dual variables, and said using a proposal generation method until no new proposals are identified;
 - [(7)] solving the integer program that includes all identified proposals; and
 - [(8)] constructing a set of winning bids from the set of winning proposals.

- 9. (Twice Amended) A program storage device readable by a machine, tangibly embodying a program of instructions executable by the machine to perform method steps for executing a combinatorial auction, said method steps comprising:
 - [(1)] reading input data comprising:
 - [(i)] a plurality of items;
 - [(ii)] a player bidding on the items; and
- [(iii)] a plurality of bids, where each bid specifies the player bidding, the amount bid, and the list of items included in the bid;
- [(2)] generating proposals by utilizing the input data, each said proposal comprising a collection of bids that can be awarded to a player participating in the auction, said bids being actual bids made and being considered simultaneously;
- [(3)] selecting a set of proposals such that each item[s] is included in at most one selected proposal; and
- [(4)] informing the players bidding on the items of the result of said selecting a set of proposals.
- 10. (Twice Amended) A computer comprising:
 - (1) means for reading input data comprising:
 - [(i)] a plurality of items;
 - [(ii)] a player bidding on the items; and
- [(iii)] a plurality of bids, where each bid specifies the player bidding, the amount bid, and the list of items included in the bid;

- (2) means for generating proposals by utilizing the input data, each said proposal comprising a collection of bids that can be awarded to a player participating in the auction, said bids being actual bids made and being considered simultaneously;
- (3) means for selecting a set of proposals such that each item is included in at most one selected proposal;
- (4) means for informing the players bidding on the items of the results in said means for selecting.